



Study on the Internal Force of Geomembrane of Landfill in Heavy Metal Contaminated Area

Hongzhou Zhang

Institute of Architectural Civil Engineering, Langfang Normal University, Langfang, 065000, China

* Corresponding author: zhanghongzhou@lfnu.edu.cn

ABSTRACT

In order to analyze the tension stress of Geomembrane in the seepage control system of a landfill in a heavy metal contaminated area under the action of the overlying landfill weight, the internal force of Geomembrane in a landfill is studied in this paper. Firstly, according to the internal force analysis of Geomembrane model, the basic equation of Geomembrane is obtained, and the equation is analyzed by finite difference numerical solution, so as to analyze the internal force of Geomembrane in a landfill. The method can analyze three stress states of Geomembrane-clay interface at different positions: elastic state, softening state and residual state, which makes the stress analysis of Geomembrane on landfill slope more reasonable. Parametric analysis shows that when the strength loss and the difference between residual displacement and peak displacement are small in the softening stage, the peak strength of Geomembrane-clay interface has little influence on the maximum tensile stress of Geomembrane and its residual strength is the main controlling factor, and when the softening characteristics of Geomembrane-clay interface are obvious, the influence of peak strength and residual displacement is more obvious.

Keywords: Geomembrane; stress; clay interface.

Estudio sobre la fuerza interna de la geomembrana del relleno sanitario en un área contaminada con metales pesados

RESUMEN

Con el fin de analizar el esfuerzo de tensión de la Geomembrana (una lamina geosintética que busca evitar la migración de contaminantes al suelo) en el sistema de control de infiltración de vertederos en áreas contaminadas con metales pesados bajo la acción del peso del vertedero suprayacente, en este documento se estudia la fuerza interna de la Geomembrana en los vertederos. En primer lugar, de acuerdo con el análisis de fuerza interna del modelo de la Geomembrana se obtiene la ecuación básica de la lámina, y la ecuación se analiza por solución numérica de diferencia finita para medir su fuerza interna en el relleno sanitario. El método puede analizar tres estados de tensión de la interfaz de Geomembrana-arcilla en diferentes posiciones: estado elástico, estado de reblandecimiento y estado residual, lo que hace que el análisis de tensión de la Geomembrana en la pendiente del vertedero sea más razonable. El análisis paramétrico muestra que cuando la pérdida de resistencia y la diferencia entre el desplazamiento residual y el desplazamiento máximo son pequeñas en la etapa de reblandecimiento, la resistencia máxima de la interfaz Geomembrana-arcilla tiene poca influencia en el esfuerzo de tensión máximo de la Geomembrana, y su resistencia residual es el principal factor de control; y cuando las características de ablandamiento de la interfaz Geomembrana-arcilla son obvias, la influencia de la resistencia máxima y el desplazamiento residual es más obvia.

Palabras clave: Geomembrana; esfuerzo; interfaz de arcilla.

Record

Manuscript received: 07/07/2019

Accepted for publication: 13/11/2019

How to cite item

Zhang, H. (2020). Study on the Internal Force of Geomembrane of Landfill in Heavy Metal Contaminated Area. *Earth Sciences Research Journal*, 24(1), 111-118. DOI: <https://doi.org/10.15446/esrj.v24n1.85231>

Introduction

Geomembrane is one of the most important components of bottom liner system and top cover system in modern sanitary landfill. It plays an important role in preventing waste leachate from polluting groundwater and protecting the surrounding environment. With the increase of landfill height, the Geomembrane in heavy metal contaminated area will produce tensile stress under the action of overlying heap weight. In order to increase the interface strength, reduce the tension stress in Geomembrane and improve the stability of landfill interface, rough Geomembrane is more and more used in landfill's slope liner system. According to the indoor shear test results, the interface of Geosynthetics-Geosynthetics and Geosynthetics-clay presents obvious strain softening characteristics. Therefore, the key to calculate the tensile stress of Geomembrane is to select the strength parameters. At present, the conventional limit equilibrium method cannot solve the tension stress of Geomembrane in the state of softening interface.

(1) The failure process of polyurea composite impervious layer in shrinkage joint is analyzed by using V-zone model (CZM). Based on the load-displacement-deformation data obtained from the debonding test of impervious layer, the interfacial stiffness and viscosity coefficient of the bonding element of the bonding layer are calibrated. In the numerical example, the critical load of coating debonding is determined, and the influence of the impervious layer's thickness of polyurea composite on the critical load of debonding is analyzed. However, when water pressure is applied to the open shrinkage joint, the thickness of the coating, the elastic modulus and the shear stress of the bonding parts will affect the debonding length of the coating, which will cause water seepage in the pit and depression areas.

(2) A generalized version of the model is created by regression fitting all size categories of the analysis unit at a given research site. The root mean square error of the corrected pic estimates ranges from 1.5% to 10.7%; these values are much better than the RMSE values of the uncorrected pic estimates. For calibrated and uncalibrated PICs, the accuracy of estimation increases with the increase of the size of the analysis unit. However, the unit size, geographic location or land's cover data set coefficients of landfills are similar, which also leads to a significant decline in the performance of the model when applied outside the development area.

(3) Based on the saturated-unsaturated seepage finite element theory, the three-dimensional seepage field of a typical earth-rock dam with random distribution of impervious Geomembrane defects is simulated. Considering the number, type, location, size and distribution of imperfections in Geomembrane, the seepage quantity of imperfections in Geomembrane and the variation law of infiltration surface behind the membrane are mainly analyzed, so as to analyze the internal force of Geomembrane according to the law of analysis. However, the interface strength model ignores the transition stage of softening, which is inconsistent with the actual situation. Therefore, it is necessary to adopt a more reasonable analysis model for the interface softening of Geomembrane to analyze the tension stress of Geomembrane on landfill slope.

In view of the above problems, this paper studies the internal force of Geomembrane on the basis of clay interface, taking landfill as the core. While describing in detail, the model of Geomembrane is constructed and its internal force is analyzed. The influence of the height, slope gradient and anchorage length of Geomembrane on the tensile stress of Geomembrane is analyzed by the cable fractional solution.

Geomembrane Model

As shown in Figure 1, Geomembrane is an important part of landfill liner system (Zhang, Weng & Shao, 2017). In order to reduce the tension stress of Geomembrane, an anchorage ditch is designed at intervals on the slope.

The unbalanced shear stress on the upper and lower surfaces of Geomembrane results in large tensile deformation of Geomembrane (Ru et al., 2018). The force acting on the Geomembrane element is shown in Figure 2.

Generally speaking, the shear strength of the interface between Geomembrane and bottom clay is the weakest in the cushion system (Lin et al., 2017), and the accumulation of shear stress will form a larger tensile stress in the anchorage ditch. This is the focus of this study. Some variables used in the analysis are shown in Figure 3.

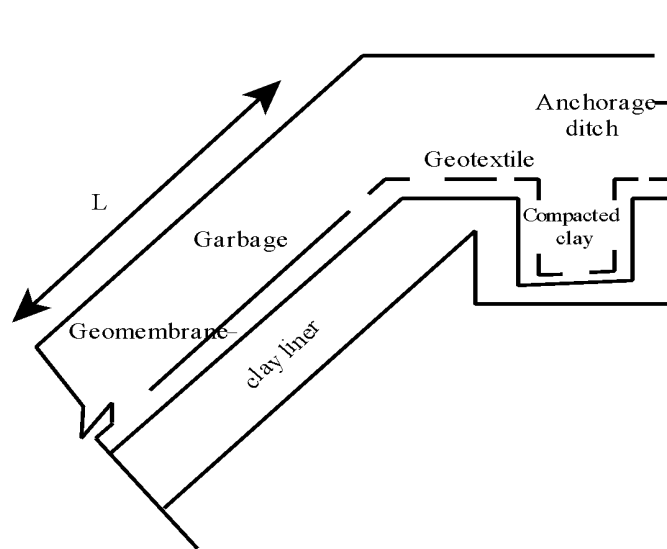


Figure 1. Typical garbage liner system

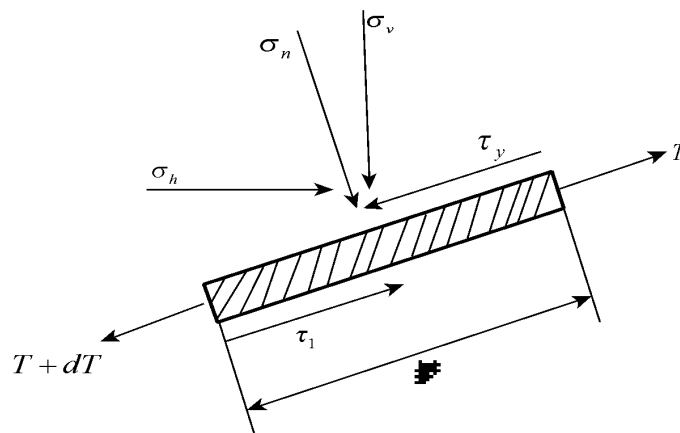


Figure 2. Stress analysis of Geomembrane element

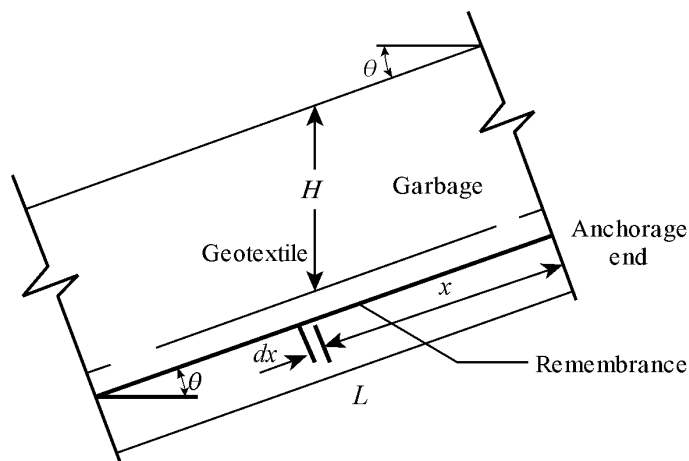


Figure 3. Variable diagram

The internal force of Geomembrane in Figure 3 is characterized by steep slope, and the overall stability of 1:3.3 rockfill dam slope is sufficient. However, the anti-sliding stability of the Geomembrane and the cement

mortar surface at its bottom depends on the bonding force between the membrane and the mortar (Huang et al., 2017). The bonding force between the membrane and the mortar is greater than 0.1 MPa if the Geomembrane is laid immediately before the cement mortar hardens and the sand bag is pressed on the membrane, so that the safety of the anti-sliding stability is sufficient. If only the friction force is used, the safety is insufficient. The anti-sliding stability between reinforced concrete slope protection and Geomembrane depends on the cohesive force of asphalt (Xu et al., 2017), which can reach 0.5 MPa, providing a high safety factor.

Usually in the design and construction, the composite Geomembrane has not been produced yet, so the polyvinyl chloride film is used. Some engineers attribute the landfill site to concrete face rockfill dam, which is very inappropriate, because the reinforced concrete mesh is not divided into blocks and without water stop sheet, it will inevitably lead to crack leakage. Polyvinyl chloride (PVC) is an impervious body, so it is appropriate to belong to Geomembrane rockfill dam. If it is attributed to the mixed dam type of Geomembrane and concrete face slab, this dam type saves the expansion joint water stop, reduces the construction difficulty greatly, saves funds, and avoids the common problem of expansion joint leakage.

Analysis of Internal Force of Geomembrane

Figure 4 is a schematic diagram of the yard structure. In this paper, all additional loads on Geomembrane are regarded as a whole and expressed as a single material. Assuming that there is no slip on the boundary surface of the upper layer of Geomembrane, i.e. $\varnothing_u > \varnothing_l$ ($\varnothing_u, \varnothing_l$) is the friction angle on the contact surface of the upper layer and the lower layer of Geomembrane respectively. The interaction between the interior of garbage and its intermediate contact layer such as the overlying soil, is ignored, so that the estimated results tend to be safe and the analysis process will be obviously simplified.

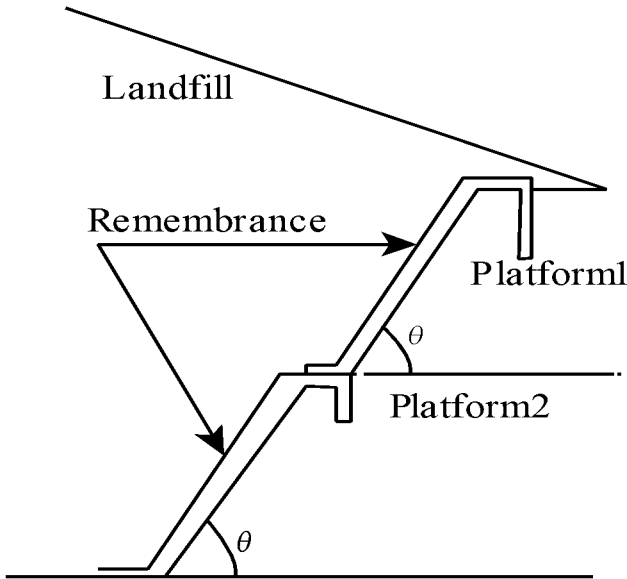


Figure 4. Diagram of landfill structure

Fundamental Equation of the Model

The shear stress on the contact surface of the Geomembrane is dependent on the shear-displacement relationship between the Geomembrane and the soil (Tang et al., 2017). It can be observed from drawing and shear tests that the shear stress τ on the contact surface increases nonlinearly with the increase of shear displacement u . In this paper, a simplified hyperbolic relationship is adopted.

$$\tau_1 = \frac{u}{a + bu} \quad (1)$$

In the formula, τ_1 is the shear stress of the contact surface of Geomembrane's lower layer; $a = 1/k_s$, k_s is the initial shear stiffness of

hyperbola; $b = 1/\tau_m$, τ_m is the ultimate shear stress of the contact surface of the Geomembrane, and $\tau_m = \sigma_n \tan \varnothing_l$.

Generally speaking, the foundation medium under Geomembrane is clay cushion (Wüthrich et al., 2018). Assuming that its shear modulus is G and its thickness is D , the clay cushion can be used to estimate k_s :

$$k_s = \frac{G}{D} \quad (2)$$

When formula (2) is substituted for formula (1) and there is no dimensionalization, it can be obtained that:

$$\frac{d^2U}{dX^2} - \frac{RU}{1+U} = \frac{A+BX}{A_1+B_1X} \quad (3)$$

Where

$$\left. \begin{aligned} u &= \frac{\tau_m}{K_x}; U = \frac{u}{u_m}; X = \frac{x}{l}; R = \frac{l^2 k_s}{E_t} \\ H^* &= \frac{H}{L}; A = -\frac{1}{2}(1-k_x)H^*R \sin 2\varnothing \\ B &= -\frac{1}{2}(1-K_x)(\sin \varnothing - \cos \varnothing \tan \beta)R \sin 2\varnothing \\ A_1 &= (K_x \cos^2 \varnothing + \sin^2 \varnothing)H^* \tan \varnothing_l \\ B_1 &= (K_x \cos^2 \varnothing + \sin^2 \varnothing)(\sin \varnothing - \cos \varnothing \tan \beta) \tan \varnothing_l \end{aligned} \right\} \quad (4)$$

In the case of small slope angle, assuming that the vertical and horizontal directions are the principal stress directions of refuse dump (Jin et al., 2017), the normal stress and active shear stress at the interface are respectively as:

$$\begin{aligned} \sigma_n &= (K_x \cos^2 \theta + \sin^2 \theta) H \gamma \\ \tau_u &= \frac{1}{2}(\sigma_v - \sigma_n) \sin 2\theta = \frac{1}{2}(1-k_x) H \gamma \sin 2\theta \end{aligned} \quad (5)$$

Because the tensile stiffness of geotextile is one order smaller than that of Geomembrane, it can be assumed that the shear stress at the Geotextile-Geomembrane interface is in the limit state, and the shear stress is as follows:

$$\tau_u = c_t + \sigma_n \tan \varphi_t \quad (6)$$

Where, c_t and φ_t are the interface strength parameters of Geotextile-Geomembrane (Choi et al., 2017). The active shear stress formula (6) and the interfacial shear stress formula (4) of Geomembrane-clay are the smaller values of the overlying shear stress of Geomembrane.

Most interface tests show that the strength of Geomembrane-clay interface presents obvious softening characteristics (Tang et al., 2017). In this paper, the tensile stress of Geomembrane on landfill slope is analyzed by using the Geomembrane-clay interface softening model as shown in Figure 5. When the relative displacement of the interface reaches the ultimate displacement u_p , the maximum shear strength τ_p is excited, and the shear strength will continue to decrease with the increase of the relative displacement. When the relative displacement reaches the residual displacement u_r , the shear strength will stabilize at the residual strength τ_r (if $u_p = u_r$, the ideal elastic-plastic solution of the softening section cannot be considered). The shear strength and relative displacement of the plane can be divided into three stages: elastic stage, softening stage and residual stage. The interfacial shear strength conforms to the Mohr-Coulomb failure criterion (McClung & Ibáñez, 2017) shown in Figure 6, in which c_p, φ_p and c_r, φ_r are the peak strength parameters and residual strength parameters of the Geomembrane-clay interface, respectively.

For the three stages of relative displacement of the above interface, formula (7) can be expressed as follows:

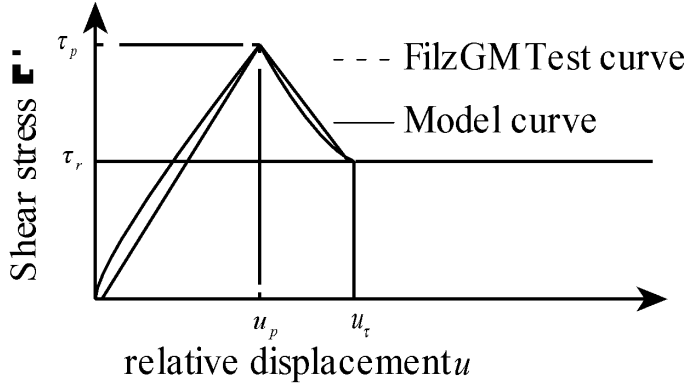


Figure 5. Softening model of Geomembrane-clay interface

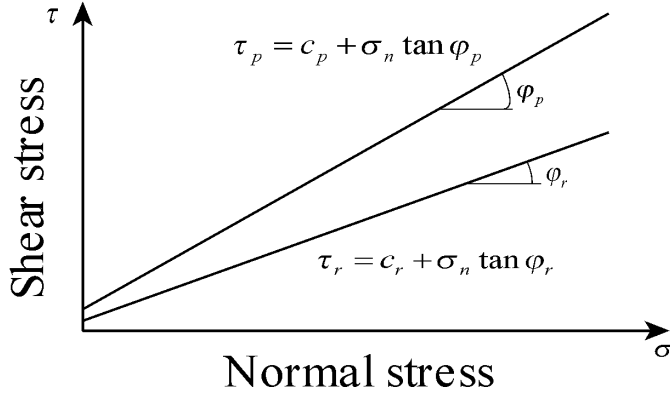


Figure 6. Mohr-Coulomb criterion for Geomembrane-clay interface

$$\left. \begin{aligned} \frac{d^2u}{dx^2} &= \frac{1}{tE}(ku - \tau_u), u \leq u_p \\ \frac{d^2u}{dx^2} &= \frac{1}{tE} \left[k'(u - u_p) + \tau_p - \tau_u \right], u_p < u \leq u_r \\ \frac{d^2u}{dx^2} &= \frac{1}{tE}(\tau_r - \tau_u), u > u_r \end{aligned} \right\} \quad (7)$$

The solutions of formula (7) are respectively

$$\left. \begin{aligned} u &= A_1 e^{ax}, A_2 e^{-ax}, u \geq u_p \\ u &= B_1 \cos bx + B_2 \sin bx + \frac{k'u_p + \tau_u - \tau_p}{k'}, u_p < u \leq u_r \\ u &= \frac{(\tau_r - \tau_u)}{2tE}x^2 + c_1x + c_2, u > u_r \end{aligned} \right\} \quad (8)$$

In the formula, the constants A_1 , A_2 , B_1 , B_2 , C_1 and C_2 depend on the boundary conditions; $A = \sqrt{K/tE}$ and $b = \sqrt{-k'/tE}$ are stiffness ratio constants. The boundary conditions at both ends of Geomembrane are respectively

$$u|_{x=0} = 0; \quad \left. \frac{du}{dx} \right|_{x=L} = 0 \quad (9)$$

Because the shear strength and relative displacement of Geomembrane-clay interface can be expressed in three stages (Li, Wu & Choi, 2017), the

Geomembrane interface can also be divided into three stages from anchoring end to free end: elastic stage ($u \leq u_p$), softening stage ($u_p < u \leq u_r$) and residual stage ($u > u_r$). In this paper, the elastic stage length is defined as L_p and the softening stage length is L_r . When $x = L_p$, $u = u_p$; when $x = L_p + L_r$, $u = u_r$. According to the boundary conditions of formula (9), formula (8) can be rewritten as

$$U = \frac{(\tau_p - \tau_u + \tau_u e^{-aL_p}) e^{ax} + (\tau_u - \tau_p - \tau_u e^{aL_p}) e^{-ax}}{K(e^{aL_p} - e^{-aL_p})} + \frac{\tau_u}{K}, \quad (10)$$

$$0 \leq x < L_p$$

$$\left. \begin{aligned} u &= \frac{(\tau_p \cos bL_p) - (u_p - u) \sin b(x - L_p)}{k' \cos bL} + \\ &\frac{k'u_p + u_p - \tau_p + (\tau_p \cos b - x_u)L(-p)}{k'} \end{aligned} \right\} \quad (11)$$

$$L_p \leq x < L_p + L_r$$

$$U = \frac{(\tau_r - \tau_u)}{2tE} [x^2 - (L_p + L_r)^2] - \frac{(\tau_r - \tau_u)}{tE} [x - (L_p + L_r)] \quad (12)$$

$$+ u_r, L_p + L_r < x \leq L$$

It is concluded that the tensile stress of Geomembrane is as follows.

$$\left. \begin{aligned} \frac{T}{tE} &= \frac{du}{dx} = \\ &\frac{(\tau_p - \tau_u + \tau_u e^{-aL_p}) ax - (u_p - u e^{aL_p}) - ax}{k(e^{aL_p} - e^{-aL_p})} \end{aligned} \right\} \quad (13)$$

$$0 \leq x < L_p$$

$$\left. \begin{aligned} \frac{T}{tE} &= \frac{du}{dx} = \frac{b(\tau_r - \tau_u) - (\tau_p - \tau_u) \cos bL_r}{k' \cos bL_r} \\ &\cos b(x - L_p) + \frac{-b(\tau_p - \tau_u) \sin b(x - L_p)}{K'} \end{aligned} \right\} \quad (14)$$

$$L_p \leq x < L_p + L_r$$

$$\left. \begin{aligned} \frac{T}{tE} &= \frac{du}{dx} = \frac{(\tau_r - \tau_u)}{tE} (x - L), \\ &L_p + L_r < x \leq L \end{aligned} \right\} \quad (15)$$

In the formula, L_p and L_r can be obtained by the internal force coordination conditions of elastic and transitional stages and the internal force coordination conditions of transitional (Fils et al., 2018) and plastic stages, respectively.

$$\left. \begin{aligned} &\frac{(\tau_p - \tau_u)(e^{aL_p} + e^{-aL_p}) + 2\tau_u}{k(e^{aL_p} - e^{-aL_p})} \\ &\frac{b(\tau_r - \tau_u) - (\tau_p - \tau_u) \cos bL_r}{k' \sin bL_r}, x = L_p \end{aligned} \right\} \quad (16)$$

$$\left. \begin{aligned} & b \frac{(\tau_r - \tau_u) \cos bL_T - (\tau_p - \tau_u)}{k' \sin bL_T} = \frac{(\tau_R - \tau_U)}{tE} \\ & (L_p + L_T - L), x = L_p + L_T \end{aligned} \right\} \quad (17)$$

Finally, the values of L_p and L_T obtained by formula (16) and formula (17) are substituted for formula (11)-(13) to obtain the tensile stresses at all points on Geomembrane. The tensile stress at $x = 0$ is the maximum tensile stress of Geomembrane (Zhang et al., 2018), and its expression is as follows:

$$T_{\max} = atE \frac{2(\tau_p - \tau_u) + \tau_u (e^{-aL_p} + e^{aL_p})}{k(e^{aL_p} - e^{-aL_p})} \quad (18)$$

Numerical Solution of Finite Difference

Because formula (18) is a non-linear differential equation, the finite difference method is used to solve it numerically. Dimensionless Geomembrane length is divided into n elements, then the number of nodes is $(n+1), i = 0, 1, 2, \dots, n$, and $\Delta X = 1/n$, and a virtual node $(n+1)$ is added to the free end of Geomembrane.

For the second order differential, the difference scheme is used:

$$\frac{\Delta^2 U}{\Delta^2 X} = \frac{U_{i=1} - 2U_i + U_{i+1}}{(\Delta X)^2} \quad (19)$$

For first order differential, the difference scheme is
At node $i = 0$,

$$\frac{\Delta U}{\Delta X} = \frac{-U_2 + 4U_1 - 3U_0}{2\Delta X} \quad (20)$$

At node $i = 1, 2, \dots, n$,

$$\frac{\Delta U}{\Delta X} = \frac{U_{i+1} - U_{i-1}}{2\Delta X} \quad (21)$$

It can be obtained by finite difference method and boundary conditions at both ends of Geomembrane.

$$T_i = \begin{cases} \frac{n\tau_m L}{2R} (4U_1 - U_2), i = 0 \\ \frac{n\tau_m L}{2R} (U_{i+1} - U_{i-1}), i = 1, 2, \dots, n \end{cases} \quad (22)$$

Based on the above method, the tension and displacement of Geomembrane can be obtained by numerical iteration (Su et al., 2019), and the influence of various parameters of landfill slope on the displacement and tension of Geomembrane can be analyzed by numerical method. In this paper, the main parameters affecting the displacement and tension of Geomembrane, inclination q , length L , elastic modulus E and height H , are studied. The results are shown in Figure 7-10. From Figure 7, it can be seen that the displacement and tension of Geomembrane are non-linear along its length. When other conditions are the same, both displacement and tension increase with the increase of inclination angle (Zhang, Dai, Liu, et al., 2017), and when q is small, the change of q has a greater impact on the tension and displacement. From Figure 7 to 10, it can be seen that the influence of the length, modulus of elasticity and height of geomembrane on the displacement and tension of Geomembrane is similar to that of dip angle q .

The peak strength $\tau_p = c_p + \sigma_n \tan \varphi_p$ of the interface between Geomembrane and clay is the maximum strength that the interface can exert when the relative displacement of the interface is u_p , and the residual strength $(\tau_r = c_r + \sigma_n \tan \varphi_r)$ is formed when the relative displacement of the interface is greater than the residual displacement u_r due to the rearrangement of clay particles on the interface or the polishing of the surface of geosynthetics. The

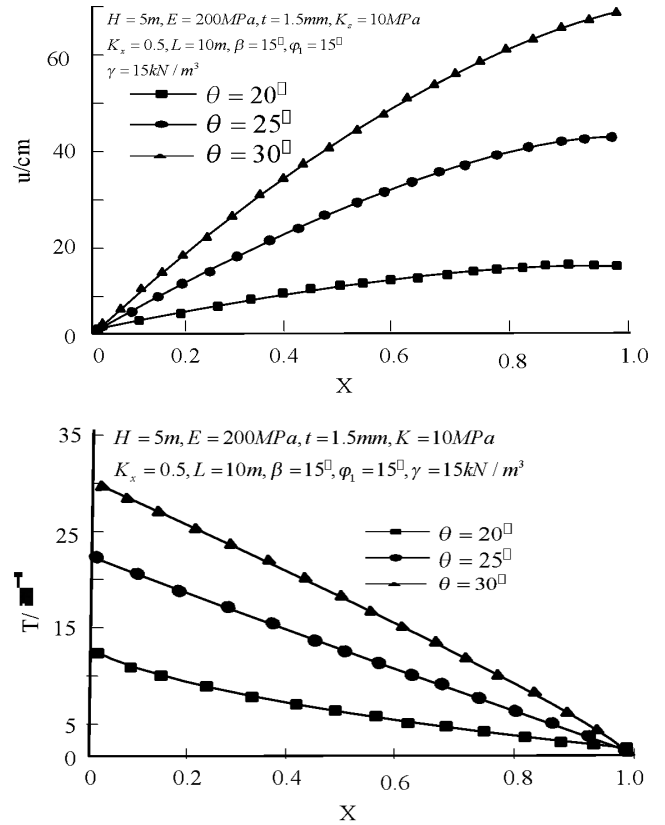


Figure 7. The influence of inclination angle q on displacement X and tension T of Geomembrane

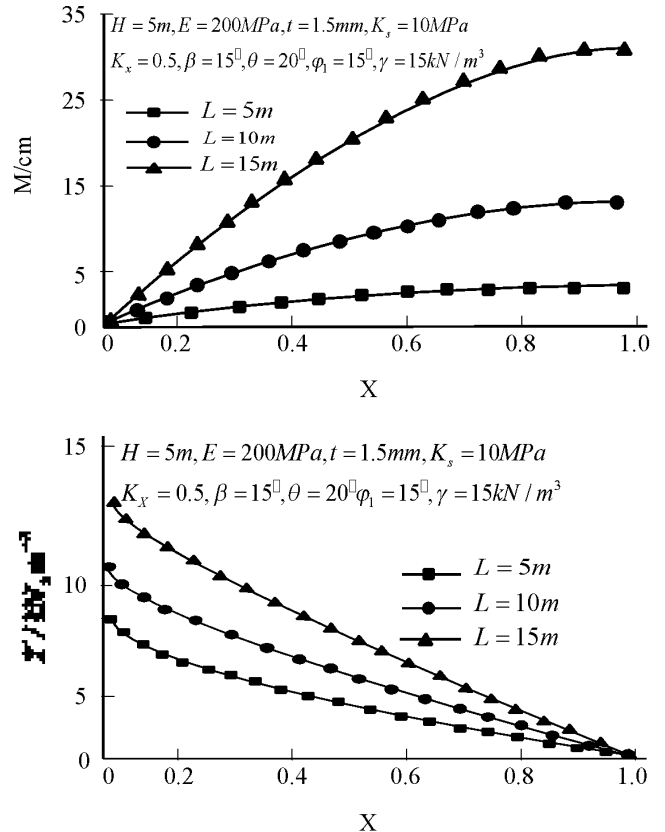


Figure 8. The influence of length L on displacement X and tension T of Geomembrane

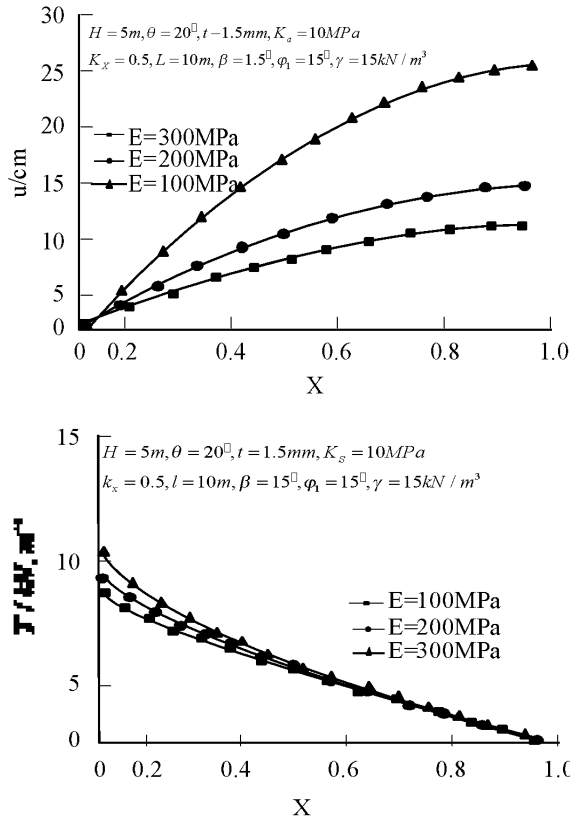


Figure 9. The influence of elastic modulus E on displacement X and tension T of Geomembrane

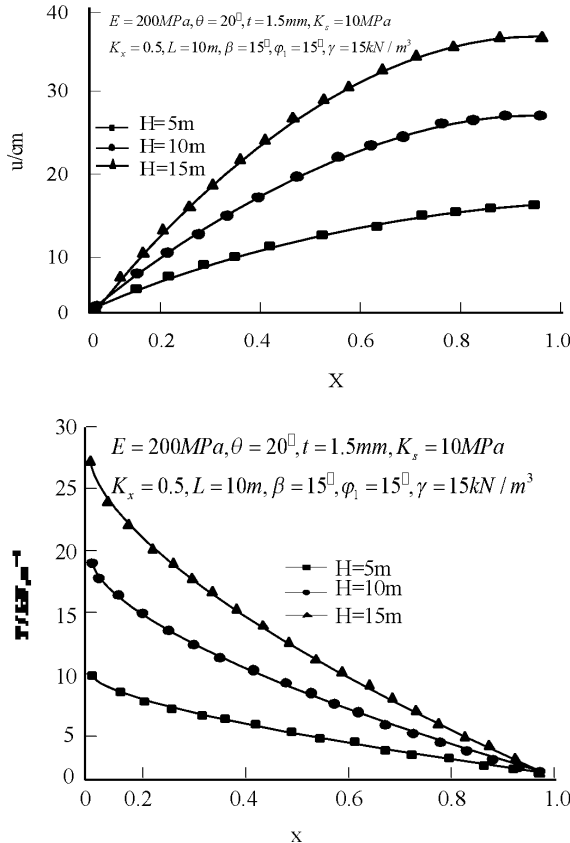


Figure 10. The influence of Height H on displacement X and tension T of Geomembrane

peak strength τ_p and residual strength τ_r of rough Geomembrane-clay interface are usually quite different. Therefore, the selection of interface strength is one of the key factors that affect the safety of Geomembrane. When the Geomembrane-clay interface enters the residual state (Figure 11), the shear stress of the Geomembrane-clay interface from anchorage to free end is elastic, softening and residual respectively. Figure 11 shows that the smaller the residual displacement u_r is, the easier the residual strength of the Geomembrane-clay interface will be. Therefore, the influence of residual displacement u_r and peak shear strength τ_p on the tensile stress of Geomembrane will be smaller (Figure 12). At this time, the exertion of surface shear stress under Geomembrane depends on the residual strength of the interface, when u_r is larger, the length of the interface between Geomembrane and clay in the softening zone is longer, and the influence of u_r and τ_p on the tensile stress of Geomembrane is more obvious. In this case, if the softening of the interface strength between Geomembrane and clay is not considered (Luo et al., 2017), the maximum tensile stress of Geomembrane obtained by the ideal elastic-plastic method according to the peak strength or residual strength of the interface will be inconsistent with the actual situation. As shown in Figure 13, it is not safe to calculate the maximum tensile stress of Geomembrane by the ideal elastic-plastic method (Erhart & Hirche, 2017). Because the difference between residual displacement u_r and peak displacement u_p is small, the influence of peak shear strength τ_p of Geomembrane-clay interface on the maximum tensile stress of Geomembrane in Figure 13 is also small. Figure 14 and Figure 15 show the tensile displacements and stresses at different positions of Geomembrane under different residual strengths. It can be seen that the residual strength seriously affects the tensile displacements and stresses of Geomembrane.

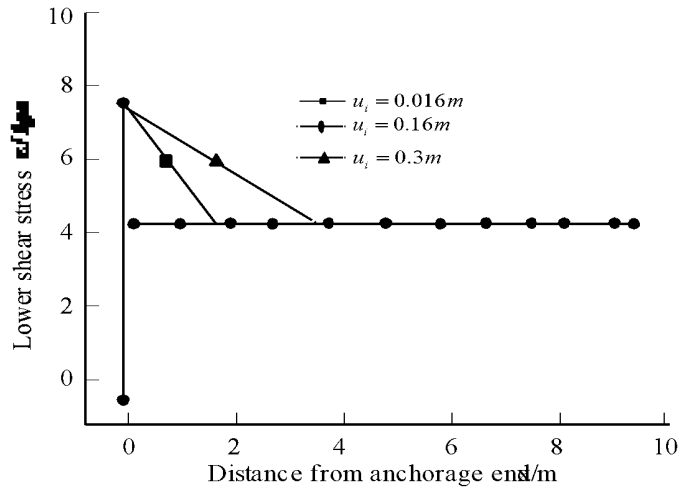


Figure 11. Curve of shear stress variation with distance under overburden

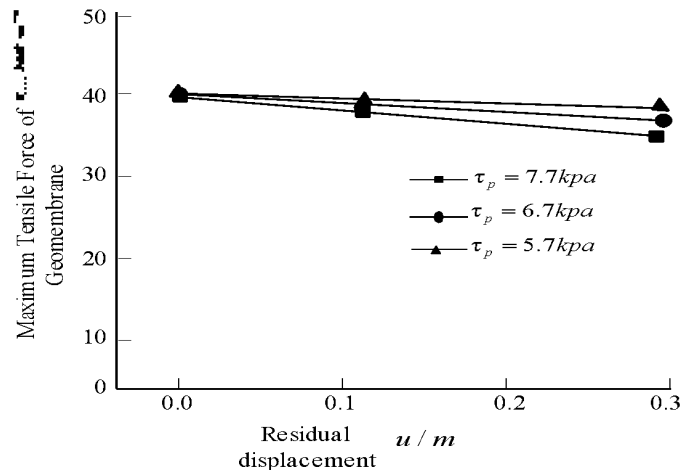


Figure 12. Effect of residual displacement on the maximum tensile stress of Geomembrane

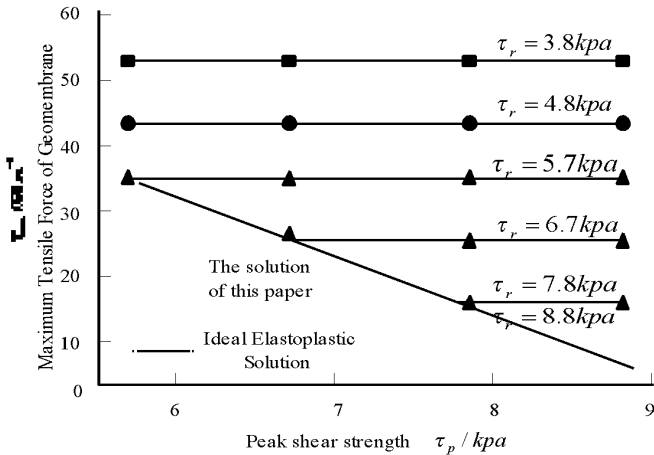


Figure 13. Effect of peak shear strength on the maximum tensile stress of Geomembrane

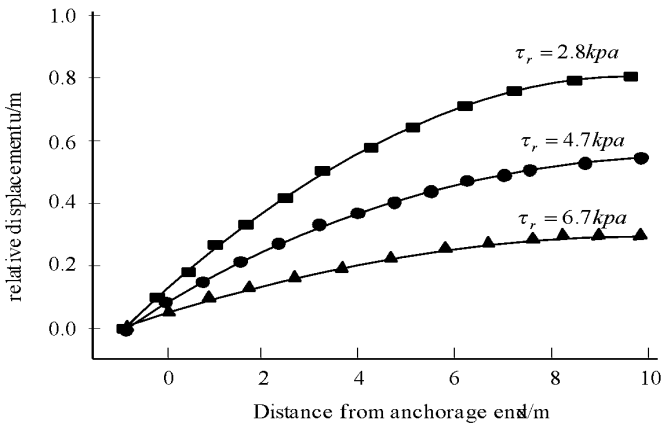


Figure 14. Curve of relative displacement variation with distance

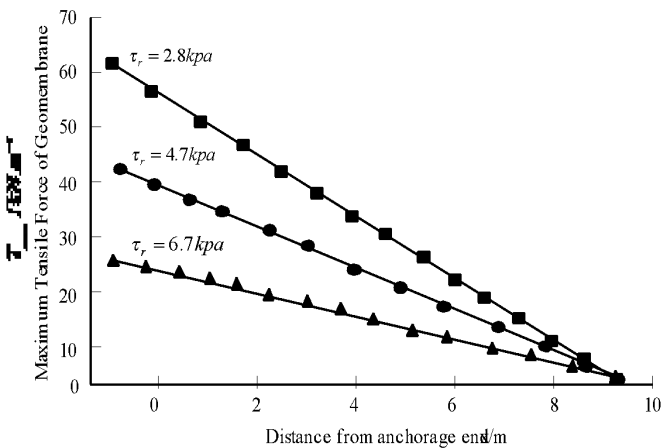


Figure 15. Curve of tensile stress in Geomembrane with distance

Simulation Experiment

The dam body is raised to 40m elevation at the original refuse dam and continued to be landfilled to 120m elevation. A horizontal anti-seepage system is added to the reservoir area in combination with the closure system of the first phase of the project and a leachate drainage system is added to the reservoir area of the first phase of the project. Some of the original sewage treatment tanks are used, and a leachate regulating tank is expanded downstream of the original sewage interception dam. Horizontal anti-seepage system consists of protective layer, leachate collection layer, main anti-seepage layer of Geomembrane,

secondary anti-seepage layer (GCL geosynthetical bentonite cushion) or clay liner (CCL), strengthening layer, clay protective layer, strengthening layer, gas conducting layer and isolation layer from top to bottom. The calculation parameters are as follows: the geotechnical composite drainage mesh-Geomembrane strength parameters are $c = 0kpa$ $\varphi = 13$, the interface parameters of Geomembrane-geosynthetical bentonite cushion are $c_p = 2.2kpa$, $\varphi_p = 21.6$, $c_r = 1.0kpa$, $\varphi_r = 12.8$, the Geomembrane-clay interface parameters are $c_p = 0kpa$, $\varphi_p = 11$, $c_r = 0kpa$, $\varphi_r = 6.5$ respectively, the landfill weight is $\gamma_{max} = 10.2kN/m^3$ and the slope gradients are $\theta = 14$, $H = 12 \sim 40m$, $L = 10m$, $u_p = 0.012m$, $u_r = 0.016m$, $t = 0.0015m$, $E = 180MPa$ $K_x = 0.56$. The maximum tensile stress of Geomembrane varies with the height of landfill as shown in Figure 16. When the Geomembrane is GCL, there is no tensile stress in the Geomembrane because the shear strength of the surface under the Geomembrane is greater than that of the surface above. When the Geomembrane is lined with clay, the lower strength of the Geomembrane-clay interface makes the Geomembrane have great tensile stress.

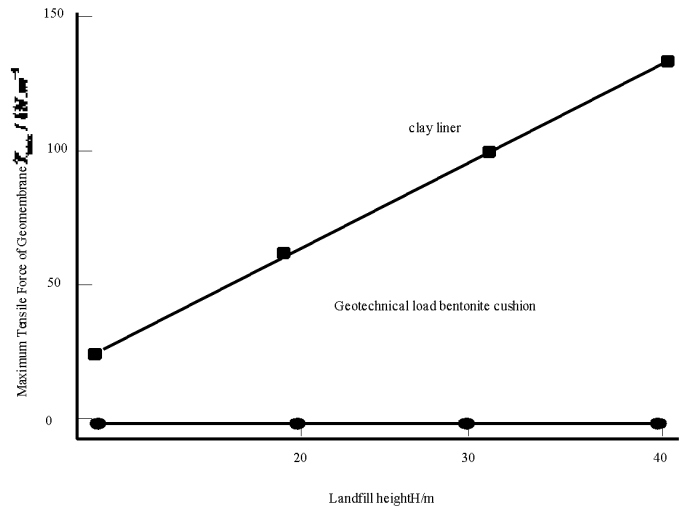


Figure 16. The influence of landfill height on the maximum tensile stress of Geomembrane

Conclusion

Based on the softening model of interface strength between Geomembrane and clay, the equilibrium equation of Geomembrane force is established, and the analytical solution of tension stress and displacement of Geomembrane is obtained. Through further parameter study, the following conclusions are drawn:

- (1) In the strength softening model of Geomembrane-clay interface, the longer the softening section is, the greater the influence of the peak strength and residual displacement of the interface on the tensile stress of geomembrane is. On the contrary, the residual strength of the interface is the main controlling factor of the maximum tensile stress of the Geomembrane when the softening stage is short.
- (2) When the strength of Geotextile-Geomembrane interface is close to or less than the residual strength of Geomembrane-clay interface, the tensile stress of Geomembrane is very small or even not.
- (3) Slope gradient, anchorage length and height of overlying pile of Geomembrane have great influence on the maximum tensile stress of Geomembrane.
- (4) The maximum tensile stress of Geomembrane can be effectively reduced by using rough HDPE Geomembrane with high interfacial strength, choosing appropriate geotextile, reducing the anchorage length of Geomembrane and limiting the height of pile on Geomembrane.

Acknowledgments:

Langfang Science and Technology Research and Development Program: Landfill Slope Geomembrane Internal Force Research in Langfang Area (2016013105)

References

- Cen, W., Du, X., Geng, L., & He, H. (2018). Seepage properties of geomembrane faced earth-rock dams under random multiple defects. *Advances in Science and Technology of Water Resources*, 38, 60-65.
- Chand, S., Crémière, A., Lepland, A., Thorsnes, T., Brunstad, H., & Stoddart, D. (2017). Long-term fluid expulsion revealed by carbonate crusts and pockmarks connected to subsurface gas anomalies and palaeochannels in the central North Sea. *Geo-Marine Letters*, 37, 215-227.
- Choi, J., Maniquiz-Redillas M. C., Hong, J., & Kim, L. (2017). Selection of cost-effective Green Stormwater Infrastructure (GSI) applicable in highly impervious urban catchments. *Ksce Journal of Civil Engineering*, 22, 1-7.
- Coronado, G. D., Rivelli, J. S., Fuoco, M. J., Vollmer, W. M., Petrik, A. F., Keast, E., Narker, S., Topalanchik, E., & Jimenez, R. (2018). Effect of Reminding Patients to Complete Fecal Immunochemical Testing: A Comparative Effectiveness Study of Automated and Live Approaches. *Journal of General Internal Medicine*, 33, 72-78.
- Erhart, S., & Hirche, S. (2017). Internal Force Analysis and Load Distribution for Cooperative Multi-Robot Manipulation. *IEEE Transactions on Robotics*, 31, 1238-1243.
- Fils, S. C. N., Mimba, M. E., Dzana, J. G., Etouana, J., Mounoumeck, P. V., & Hakdaoui, M. (2018). TM/ETM+/LDCM Images for Studying Land Surface Temperature (LST) Interplay with Impervious Surfaces Changes over Time Within the Douala Metropolis, Cameroon. *Journal of the Indian Society of Remote Sensing*, 46, 131-143.
- Gholamreza, S., Mousa, A., & Meguid, M. A. (2017). Plausible failure mechanisms of wildlife-damaged earth levees: insights from centrifuge modeling and numerical analysis. *Canadian Geotechnical Journal*, 54, 1496-1508.
- Huang, W. C., Ali, F., Zhao, J., Rhee, K., Mou, C., & Bettinger, C. J. (2017). Ultrasound-Mediated Self-Healing Hydrogels Based on Tunable Metal-Organic Bonding. *Biomacromolecules*, 18, 1162-1171.
- Jin, W., Wu, Z., Wu, C., Cao, Z., Fan, W., & Tarolli, P. (2017). Improving impervious surface estimation: an integrated method of classification and regression trees (CART) and linear spectral mixture analysis (LSMA) based on error analysis. *Giscience & Remote Sensing*, 55, 1-21.
- Kaiser, P., Schmoelz, W., Schoettle, P., Zwierzina, M., Heinrichs, C., & Attal, R. (2017). Increased internal femoral torsion can be regarded as a risk factor for patellar instability - A biomechanical study. *Clinical Biomechanics*, 47, 103-109.
- Lin, B., Yang, X. Z., Cao, X. W., Zhang, T. Z., Wang, F. J., & Zhao, J. (2017). A novel trichosanthin fusion protein with increased cytotoxicity to tumor cells. *Biotechnology Letters*, 39, 1-8.
- Li, B., Zhang, Y., Liu, X., Li, Z. (2017). Study on the polyurea-coat debonding failure of impervious structure in contraction joints. *Journal of Hydraulic Engineering*, 48, 70-77.
- Li, W., Wu, C., & Choi, W. (2017). Predicting future urban impervious surface distribution using cellular automata and regression analysis. *Earth Science Informatics*, 11, 1-11.
- Luo, Y., Nie, M., & Xiao, M. (2017). Flume-scale experiments on suffusion at bottom of cutoff wall in sandy gravel alluvium. *Canadian Geotechnical Journal*, 54:1716-1727.
- Mccclung, T., & Ibáñez, I. (2017). Quantifying the synergistic effects of impervious surface and drought on radial tree growth. *Urban Ecosystems*, 21, 1-9.
- Ostfeldt, C., Beguin, J. S., Pedersen, F. T., Polzik, E. S., Muller, J. H., & Appel, J. (2017). Dipole force free optical control and cooling of nanofiber trapped atoms. *Optics Letters*, 2017, 42:4315-4318.
- Parent, J. R., & Qian, L. (2018). Estimating percent impervious cover from Landsat-based land cover with a simple and transferable regression model. *International Journal of Remote Sensing*, 39, 3839-3851.
- Ru, X., Zhang, H., & Hui, L. (2018). Annual dynamics of impervious surfaces at city level of Pearl River Delta metropolitan. *International Journal of Remote Sensing*, 39, 3537-3555.
- Su, H., Cui, S., Wen, Z., & Xie, W. (2019). Experimental study on distributed optical fiber heated-based seepage behavior identification in hydraulic engineering. *Heat and Mass Transfer*, 55:421-432.
- Tang, J., Di, L., Xiao, J., Lu, D., & Zhou, Y. (2017). Impacts of land use and socioeconomic patterns on urban heat Island. *International Journal of Remote Sensing*, 38:3445-3465.
- Wüthrich, D., Pfister, M., Nistor, I., & Schleiss, A. J. (2018). Experimental study on the hydrodynamic impact of tsunami-like waves against impervious free-standing buildings. *Coastal Engineering Journal*, 60, 180-199.
- Xu, Z., Mountrakis, G., & Quackenbush, L. J. (2017). Impervious surface extraction in imbalanced datasets: integrating partial results and multi-temporal information in an iterative one-class classifier. *International Journal of Remote Sensing*, 38, 43-63.
- Zhang, L., Shan, B., Zhao, Y., & Tang, H. (2018). Comprehensive Seepage Simulation of Fluid Flow in Multi-scaled Shale Gas Reservoirs. *Transport in Porous Media*, 121:263-288.
- Zhang, L., Weng, Q., & Shao, Z. (2017). An evaluation of monthly impervious surface dynamics by fusing Landsat and MODIS time series in the Pearl River Delta, China, from 2000 to 2015. *Remote Sensing of Environment*, 201:99-114.
- Zhang, W., Dai, B., Liu, Z., & Zhou, C. (2017). Unconfined Seepage Analysis Using Moving Kriging Mesh-Free Method with Monte Carlo Integration. *Transport in Porous Media*, 116, 163-180.