

Pitch Angle Control for Variable Speed Wind Turbines

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Abstract - Pitch control is a practical technique for power regulation above the rated wind speed it is considered as the most efficient and popular power control method. As conventional pitch control usually use PI controller, the mathematical model of the system should be known well. This paper deals with the operation and the control of the direct driven permanent magnet synchronous generator (PMSG).

Different conventional strategies of pitch angle control are described and validated through simulation results under Matlab\Simulink.

Keywords - variable-speed wind turbine; MPPT; pitch control; PMSG.

Nomenclature –

PMSG	Permanent magnet synchronous generator
HAWT	Horizontal-axis wind turbines
VAWT	Vertical axis wind turbines
TSR	Tip speed ratio
MPPT	Maximum Power Point Tracking
PWM	Pulse width modulation
PI	Proportional integral

I. INTRODUCTION

Traditional energy resources, especially from fossil origins, will break off in the following few decades, which predict an energy shortage in the world. In addition, the energy consumption, in its various forms, increased in an exponential way. To satisfy these needs, it was necessary to solve this problem. Actually, there was a simple way to do so, since there were inexhaustible renewable energy resources, which can be easily and properly exploited [1-3]. Nevertheless, being neglected for a long time, power extraction techniques of these resources requires more researches and developments aiming to make the manufacturing costs reliable and lower and to increase the energy efficiency [4-5].

In this general context, this study was interested in the wind energy which seems to be one of the most promising energies with a very high rate growth in the world. Today, the wind power has become a

reality with the increase of the installed power all over the world a significant proportion of this type of energy is available in windy areas.

Recently, pitch-adjusting variable-speed wind turbines have become the dominating type of installed wind turbines. Pitch angle control method is a basic approach to improve the performance of the power generation system including different types of wind turbines. Although a wind turbine can be built in either a vertical-axis or horizontal-axis configuration, we focus on horizontal-axis wind turbines (HAWTs) because they dominate the utility-scale wind turbine market. At the utility scale, HAWTs have aerodynamic and practical advantages [6]. Smaller vertical axis wind turbines (VAWTs) are more likely to use passive rather than active control strategies. In fact, generally for vertical axis wind turbine, which consists of several blades rotating about axis in parallel direction, the cycloid blade system and the individual active blade control system are adopted.

Both methods are variable pitch system. For cycloid wind turbine, aerodynamic analysis is carried out by changing pitch angle and phase angle based on the cycloid motion according to the change of wind speed and wind direction. And for more efficient wind turbine, individual pitch angle control of each blade is obtained by maximizing the tangential force in each rotating blade at the specific rotating position, optimal.

Therefore, generally for the variable-speed wind turbines two controllers are used. Below rated value, in low wind speed, the speed controller can continuously adjust the rotor speed to maintain the tip speed ratio constant at the level which gives the maximum power coefficient, so the efficiency of the turbine will be significantly increased. Pitch angle regulation is necessary in conditions above the rated wind speed when the rotational speed is kept constant which can have a dramatic effect on the power output. The purpose of the pitch angle control might be expressed as follows [7-8]:

- Optimizing the wind turbine power output. Below rated wind speed, the pitch setting should be at its optimum value to give maximum power.
- Preventing the mechanical power input to beat the design limits. Above rated wind speed, pitch angle control provides an effective method of regulating the aerodynamic power and loads produced by the rotor.
- Minimizing fatigue loads of the turbine mechanical component. It is clear that the action of the control system can have a major impact on the loads experienced by the turbine. The design of the controller must take into account the effect on loads, and the controller should ensure that excessive loads will not result from the control action. It is possible to go further than this, and explicitly design the controller with the reduction of certain fatigue loads as an additional objective.

In this paper, conventional pitch angle control strategy in which various controlling variables may be used is discussed.

II. WIND TURBINE MODELING

In order to simulate the behavior of the wind turbine, it is necessary to determine the torque exerted on its shaft. The mechanical power extracted from the wind turbine is expressed by [9-10]:

$$P_w = \frac{1}{2} \rho A R^2 V_w^3 C_p(I, b) \quad (1)$$

The power coefficient C_p depends on the pitch angle of rotor blades β and the tip speed ratio (TSR) λ , with [11]:

$$C_p(\lambda, \beta) = 0.53 \left[\frac{151}{\lambda_i} - 0.58\beta - 0.002\beta^{2.14} - 13.2 \right] \times \exp\left(\frac{-18.4}{\lambda_i}\right) \quad (2)$$

Where:

$$\lambda_i = \frac{\lambda}{1 - 0.02b} - \frac{0.003}{b^3 + 1} \quad (3)$$

$$\lambda = \frac{RW}{V_w} \quad (4)$$

The turbine torque is then defined as the ratio of the mechanical power to the rotational speed:

$$T_m = \frac{P_w}{W} \quad (5)$$

The mechanical speed of the turbine is determined from the fundamental equation of the dynamics as:

$$J \frac{dW}{dt} = T_m - T_{em} - fW \quad (6)$$

The wind turbine speed is controlled in order to extract the maximum power from the wind. According to the Betz theory, the maximum power extractable from a wind turbine is 59.3% of the available wind power, which corresponds to the Betz limit with a power coefficient of 0.593 [12].

For the wind turbine modeled in this study, the curve of C_p versus λ with $b=0$, represented in Fig. 1, shows an optimum value of the TSR ($\lambda_{opt} = 8$) corresponding to a maximum value of the power coefficient ($C_{pmax} = 0.473$).

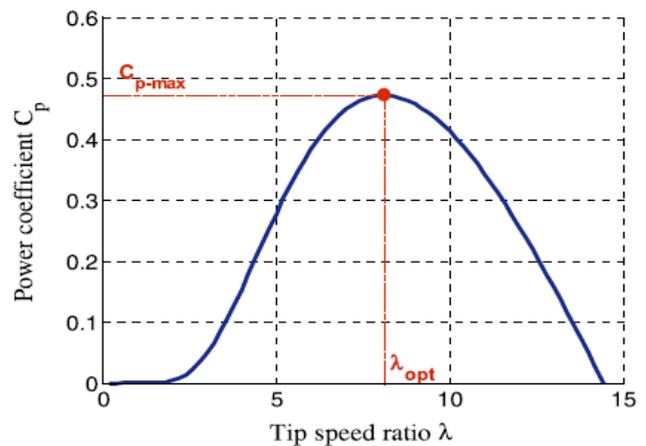


Fig .1. C_p versus λ curve

A. Control of the Wind Generator

The control of the generator power is obtained by the control of the PMSG electromagnetic torque T_{em} . The role of the pitch control system is to limit the rotational speed of the shaft, the reference electromagnetic torque T_{em-ref} , can be developed in this method [13]: The strategy of an operating at maximum power, goals to develop the turbine aerodynamic output, aiming to extract the maximum of wind power derived when the turbine operates at maximum power coefficient.

Equation 7 gives the expression of the maximum power obtained using the Maximum Power Point Tracking (MPPT) strategy which adjust automatically the ratio speed at its optimum value , I_{opt} , in order to attain the maximum power coefficient C_{pmax} , the equation below indicates the relationship between turbine power and turbine speed at maximum power. When regulating the system under the specification of maximum power, it must be considered that turbine power must never be upper than generator rated power. The output power must be limited when generator rated power is attained at rated wind speed.

$$P_{MPPT} = K_{opt} \Omega^3 \tag{7}$$

$$K_{opt} = \frac{1}{2} \frac{r p R^5 C_{pmax}}{I_{opt}^3} \tag{8}$$

In the case of high wind, it is necessary to limit the rotational speed to avoid the damage of the turbine and the electric machine. This limitation is obtained by the control of the pitch angle β .

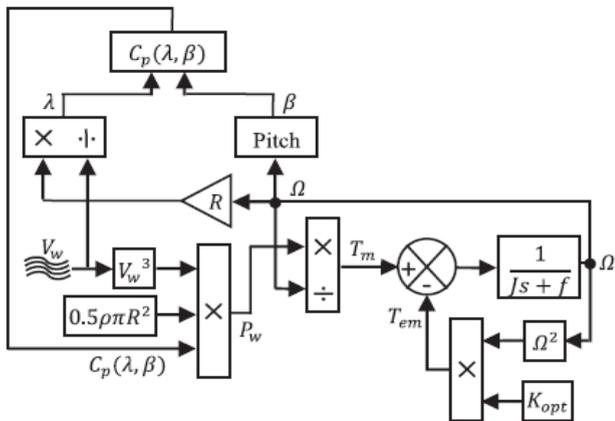


Fig .2. Turbine model

B. Wind Turbine Operating Regions

The Typical power control regions of wind turbine are shown in Figure 3. Three wind speeds are considered as limits of this division, the cut-in wind speed v_{cut-in} , the rated wind speed v_{rated} and the cut-out wind speed $v_{cut-out}$. For the wind turbine model considered in this study the values of v_{cut-in} , v_{rated} and $v_{cut-out}$ respectively are 6m/s, 10m/s and 13m/s. In region I, the wind turbine is at stop state and the pitch angle usually is set to 90° . In the partial load region, region II, the wind speed is limited between

v_{cut-in} and v_{rated} . The main objective of the control in this region is maximizing power generated by the wind turbine. The principle control objective in the full load region, region III, is maintaining the generator power P_g around the rated generator power $P_{g,rated}$.

In fact, in the case of high wind, it is necessary to limit the rotational speed to avoid the damage of the turbine and the electric machine. This limitation is obtained by the control of the pitch angle β .In region IV where the wind speed is upper than $v_{cut-out}$, the wind turbine must be shut down in order to protect wind turbine against the stresses and fatigue damages. In this case, the pitch angle usually is set to 90° and power generation is stopped. The focus of this paper is on full load region (region III) to design an optimal pitch controller.

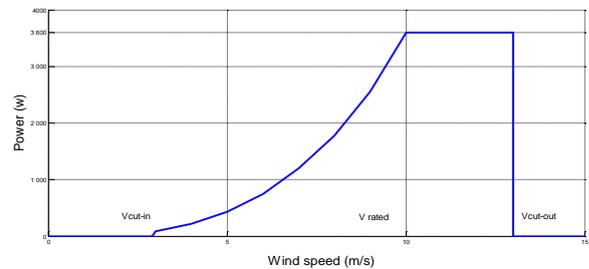


Fig .3. Wind Turbine operating regions

III. PITCH ANGLE CONTROL

The pitch control method is a basic approach for controlling the rotational speed of wind turbine. The conventional blade pitch angle control strategies are developed in this part. The pitch angle reference β_{ref} , is controlled by the input values, which may be as follows:

- Wind speed, as shown in Fig. 5(a). Perfectly, the pitch angle reference can be illustrated from the curve of the pitch angle versus wind speed, as shown in Fig.3. The direct measure of the wind speed makes this control strategy simple; however this is not a pertinent procedure, because it is difficult to measure the wind speed precisely. In fact, when the rotor speed exceeds the maximum rotor speed of turbine Ω_{tn} , the pitch angle is increased to reduce the turbine torque C_t .

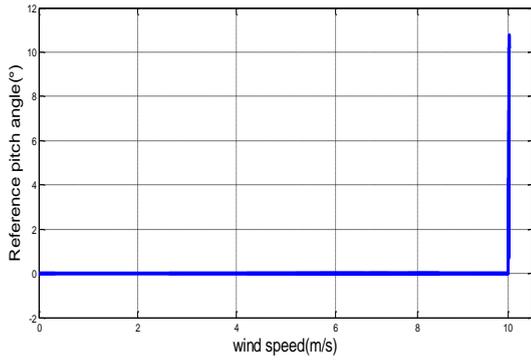


Fig .4. Reference Pitch angle

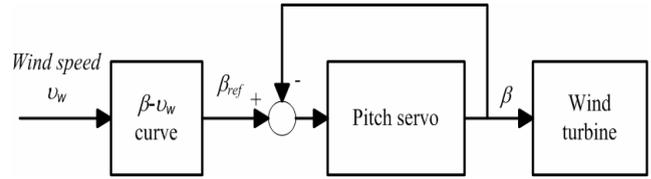
- Generator rotor speed, as shown in Fig. 5(b). The controlling rotor speed is compared with its reference. The error signal is then sent to the PI controller and produces the reference value of the pitch angle.
- Generator power, as shown in Fig. 5(c). The error signal of the generator power is sent to a PI controller. The PI controller produces the reference pitch angle b_{ref} .

For variable-speed wind turbines, a mechanical actuator is generally used to adjust the pitch angle of the blades in order to decrease the power coefficient C_p and maintain the power at its rated value. By linearization of the model to order 1 [14-16], the torque has been considered proportional to rotational speed of the turbine. The control strategy implemented is as follows:

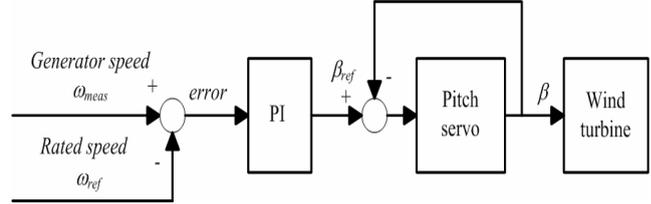
$$\begin{cases} \beta_{ref} = \beta_0 = 0 & \text{for } 0 < \Omega_t < \Omega_m \\ \beta_{ref} = \frac{\Delta\beta}{\Delta\Omega}(\Omega_t - \Omega_m) + \beta_0 & \text{for } \Omega_t > \Omega_m \end{cases} \quad (9)$$

With β_0 is the initial pitch angle (optimal value) and Ω_m (rad/s) is the nominal mechanical turbine speed. Taking into account the blades orientation system which can be hydraulic or electric type, a transfer function of the first order is introduced in order to control the position of the blades according to a reference.

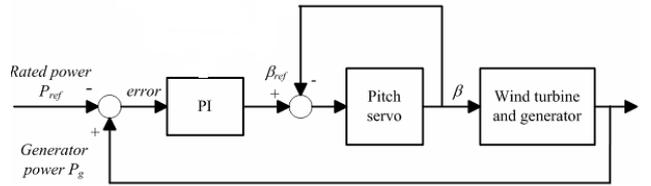
$$b = \frac{1}{1 + t_b s} b_{ref} \quad (10)$$



(a)



(b)



(c)

Fig .5. Pitch control strategy.(a) Wind speed; (b) generator rotor speed; (c) generator power

IV. PERMANENT- MAGNETIC SYNCHRONOUS GENERATOR AND RECTIFIER

A. Modeling of the PMSG

In this study a PMSG Park model is used, only the fundamental harmonic of the flux distribution in the air-gap of the machine is considered and the homopolar component is neglected, so the theory of the space vector gives the dynamic equations of the stator currents as follows:

$$\begin{cases} \frac{di_{sd}}{dt} = \frac{1}{L_s}(v_{sd} - R_s i_{sd} + L_s p \Omega_t i_{sq}) \\ \frac{di_{sq}}{dt} = \frac{1}{L_s}(v_{sq} - R_s i_{sq} - L_s p \Omega_t i_{sd} - p \Omega_t \varphi) \end{cases} \quad (11)$$

Where the phase resistance of the stator winding (Ω), the stator cyclic inductance (H), φ is the flux of the permanent magnetic (Wb), v_{sd} and v_{sq} are the d-q components of the stator voltages respectively (V), i_{sd} and i_{sq} are the d-q components of the stator currents respectively (A), and finally p is the number

of pairs of poles The electromagnetic torque is given by:

$$C_{em} = p\phi i_{sq} \tag{12}$$

B. Modeling of the Rectifier

For the dynamic model of the system, we will divide the study of the converter to three parts: the alternative part, the discontinuous part which is composed by switches and the DC side. In this context, the function of switches is to establish a connection between the AC side and the DC bus; these switches are complementary, their state is defined by the following function:

$$S = \begin{cases} +1 \\ -1 \end{cases} \text{ for } S=a,b,c \tag{13}$$

Then, the input phase voltages and the output current may be written in function of S_j , U_{dc} and input currents i_a, i_b, i_c .

$$i_a + i_b + i_c = 0 \tag{14}$$

The phase between the input PWM rectifier voltages can be described by:

$$\begin{aligned} U_{Sab} &= (S_a - S_b)U_{DC} \\ U_{Sbc} &= (S_b - S_c)U_{DC} \\ U_{Sca} &= (S_c - S_a)U_{DC} \end{aligned} \tag{15}$$

The voltage equations of the system can be written as follows:

$$\begin{bmatrix} e_a \\ e_b \\ e_c \end{bmatrix} = R \cdot \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + L \cdot \frac{d}{dt} \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + \begin{bmatrix} U_{Sa} \\ U_{Sb} \\ U_{Sc} \end{bmatrix} \tag{16}$$

Avec:

$$\begin{aligned} U_{Sa} &= \frac{2S_a - S_b - S_c}{3} U_{DC} \\ U_{Sb} &= \frac{2S_b - S_a - S_c}{3} U_{DC} \\ U_{Sc} &= \frac{2S_c - S_a - S_b}{3} U_{DC} \end{aligned} \tag{17}$$

Finally, we deduce the equation coupling between AC and DC sides by:

$$C \frac{dU_{Dc}}{dt} = S_a i_a + S_b i_b + S_c i_c \tag{18}$$

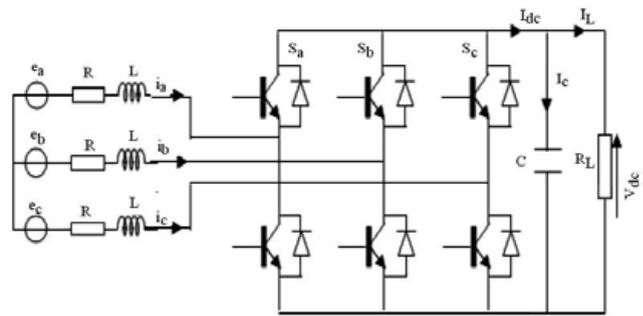


Fig .6. Diagram of MSAP- PWM Rectifier

C. Control

For variable-speed wind turbine, the maximum power is a cubic function of rotational speed. the development of the generator torque is based on the stator q-axis current component, but a freedom degree remains to set direct current. In order to minimize current for a given torque, and therefore, minimize resistive losses the direct-axis current component can be set at zero [17]. Thus, the control of the generator torque depends directly of the quadrature current component. The schematic diagram of the control loops of the permanent-magnet generator-side converter is illustrated on Fig. 7. The required d-q components of the rectifier voltage vector are determinate from two proportional plus integral (PI) current controllers: the first one is controlling the d-axis component of the current and the other one is controlling the q-axis component. In order to improve the dynamic response, compensation terms are added. The control requires the measurement of the stator currents, dc voltage, and rotor position.

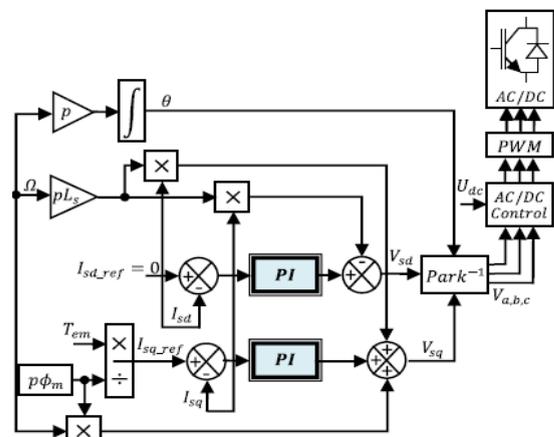


Fig .7. PMSG and converter control

D. Simulation Results and Discussion

Pitch angle control systems of the wind turbine were simulated using MATLAB/SIMULINK tool to test the control strategy and evaluate the performance of the system. The wind model is necessary to obtain realistic simulations of the power control of the wind turbines [18]. During 300 s, we have applied to the wind turbine model a variable wind profile between 6 and 12 m/s with an average value of 10 m/s. This sequence is obtained by adding a turbulent component to a slowly varying signal represented in Fig.8.

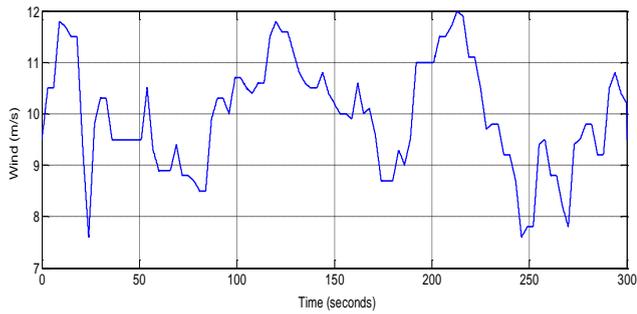


Fig .8. Wind speed

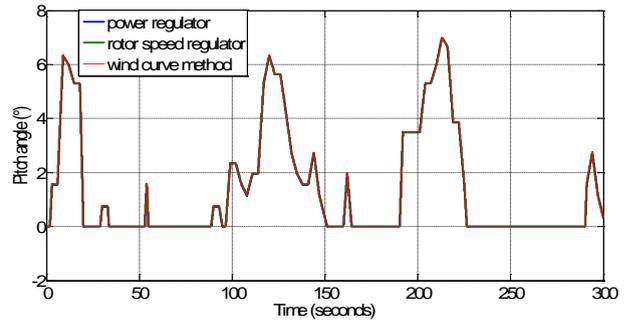


Fig .11. Pitch angle curve

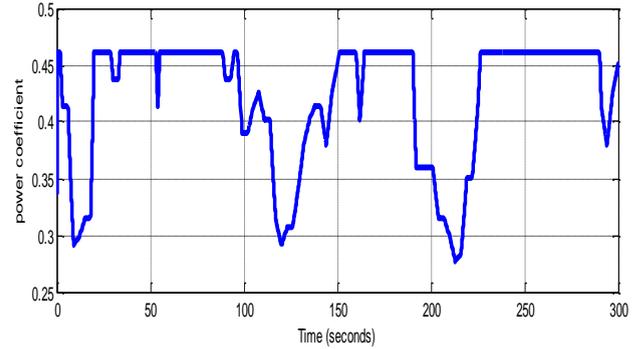


Fig .12. Power Coefficient

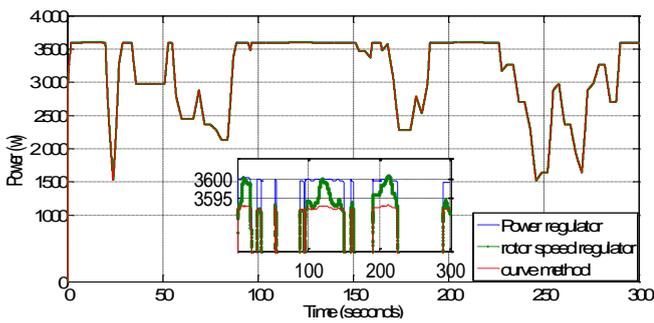


Fig .9. Output power

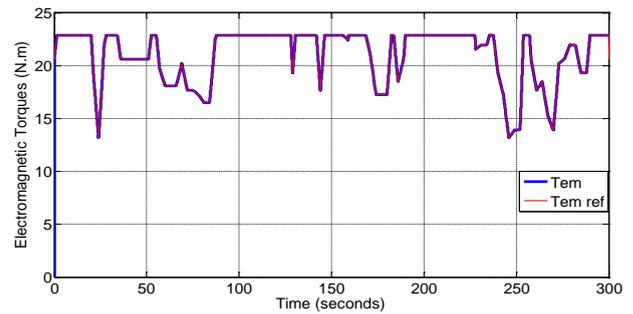


Fig .13. Electromagnetic Torque

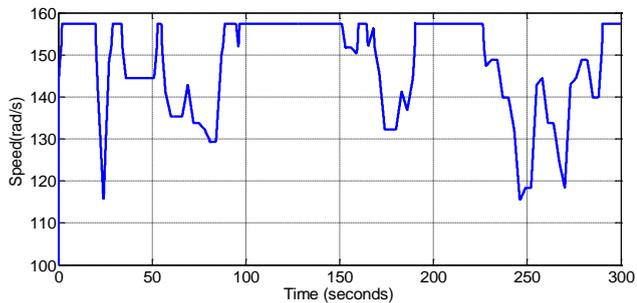


Fig .10. Mechanical speed

The wind turbine is dimensioned to provide a nominal power at a nominal speed of 10 ms⁻¹. Beyond this wind, it is necessary to protect the wind turbine against mechanical failures; therefore, we must limit its speed. This limitation will be obtained by a pitch control. The mechanical speed of the turbine represented in Fig. 10 is obtained next to the variation of the pitch angle illustrated in Fig. 11. The more the pitch angle increases, the more the power coefficient decreases (Fig. 12). The comparisons of different strategies illustrated in the simulation results show that pitch angle control strategy where the generator power is used as the controlling variable has a rapid pitch angle respond to the wind speed variation and minimum power ripples.

The response of the second strategy where rotor speed is used as the controlling variable has a squared error evaluated of 0.79 and the error of the

Response obtained next to the wind curve pitch control method is evaluated of 0.95, these results highlight the robustness of the strategy of the generator power controller.

V. CONCLUSION

In order to handle the pitch control in wind turbines, in this paper conventional methods are proposed. In fact, pitch angle control has an effect on the aerodynamic loads which may be controlled by the controller to achieve lower torque peak as well as lower fatigue loads. The simulation results show that the power controller has lower torque peak and lower power peak.

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Engineering (CASE): pp. 1–4.

APPENDIX

- Wind turbine
Dry friction torque : $C_s = 953 \text{ Nm}$
Number of blades : 3
Viscous friction coefficient : $f = 10 \cdot 3 \text{ N.m.s.rad}^{-1}$
Total inertia of the mechanical transmission: $J = 99 \cdot 10^{-4} \text{ kg.m}^2$
- PMSG
Nominal power: $P_n = 3.6 \text{ kW}$
Number of pole pairs: $p=4$
Self-inductance: $L_s = 15.1 \text{ mH}$
Permanent magnetic flux: $\Phi_a = 0.5 \text{ Nm/A}$
Stator resistance: $R_s = 0.82 \Omega$